STOCHASTIC MODELS FOR OPERATIONS RESEARCH  
Math 424 (01:640:424)

Time and Location:

Lecturer:

Office: 
Email: 
Web Page: 
Office Hours: 

Prerequisites: Probability Theory (01:640:477 or 01:960:381)


Course Webpage: [http://www.math.rutgers.edu/courses/424/](http://www.math.rutgers.edu/courses/424/)

Homework: There will be six homework assignments. Late homework will not be accepted unless it is the result of an officially excused absence.

Exams: There will be one eighty-minute midterm exam and a three-hour cumulative final exam. Exams will be closed book and student-prepared formula sheets will not be permitted. An official formula sheet will be provided with each exam. The dates of the exams listed below are tentative. The actual dates will be announced in class. Make-up exams will be allowed provided that you can supply acceptable written evidence, and that you notify the lecturer *as soon as possible*.

Midterm Exam: To be announced.
Final Exam: To be announced.

Grading: The term grade will be based on the results of the examinations, and on the performance on the homework assignments. In summary, here are the components of the term grade:

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<th>Component</th>
<th>Percentage</th>
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<td>Homework</td>
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<tr>
<td>Midterm exam</td>
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<td>Final exam</td>
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Absences: You are expected to attend every class. An absence due to illness or family emergency may be excused, provided that you can supply acceptable written evidence if required, and that you notify the lecturer as soon as possible.

Course Outline:

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General Information:

Markov chains: definition, transition probabilities, special Markov chains (random walks, dams and inventories, branching processes), classification of states, limit theorems. Poisson processes: derivations, homogeneous, non-homogeneous processes, spacial and marked Poisson processes. Continuous time Markov chains: the Chapman-Kolmogorov equation, birth and death processes, the case of a finite state space, special cases, limiting behavior. Renewal processes: definition, the renewal function, replacement models, renewal theorems, inspection paradox, applications. Brownian motions: definition, processes with independent increments, the maximum variable and the reflection principle, Brownian bridge, geometric Brownian motion, applications in modern financial theory, Black-Scholes-Merton (BSM) formula for European call option. Queueing theory: queueing systems, Littles formula, Poisson arrivals and exponential and general service times, the case of an infinite number of servers, priority queues, queueing systems.
**Homework Assignments:** Additional homework problems will be assigned in class. Suggested homework problems are the following. Show your work to get full credit.

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| 5        | Page 425 : Exercise 1.4  
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Page 437 : Problem 3.5 **Hint:** Take $T = (-\infty, \infty)$. |
| 6        | Page 555 : Exercise 2.1  
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