1. Combinatorics
   
   (a) **Enumeration**
   Binomial and multinomial coefficients, Stirling’s formula, recursions and generating functions, inclusion-exclusion principle
   
   (b) **Posets and Lattices**
   Dilworth’s theorem, LYM inequality, Sperner’s theorem, Mobius inversion formula, Birkhoff’s representation theorem, Weisner’s theorem, geometric lattices
   
   (c) **Hypergraphs**
   
   (d) **Ramsey Theory**
   Ramsey’s theorem, Van der Waerden theorem
   
   (e) **Discrepancy Theory**
   Beck-Fiala theorem

2. Graph Theory
   
   (a) **Matching Theory**
   Konig’s theorem, Hall’s marriage theorem, Tutte’s 1-factor theorem, Petersen’s theorem, Birkhoff-von Neumann theorem
   
   (b) **Connectivity**
   Menger’s theorem
   
   (c) **Planarity**
   Euler’s formula, Kuratowski’s theorem, Wagner’s theorem
   
   (d) **Coloring**
   Five color theorem, Brooks’ theorem, Konig’s theorem, Vizing’s theorem, perfect graph, list coloring, Galvin’s theorem
   
   (e) **Flows**
   Max-flow min-cut theorem
   
   (f) **Extremal Graph Theory**
   Turan’s theorem, regularity lemma, counting lemma, Erdos-Stone theorem

3. Probabilistic Method
   
   (a) **Basics**
   Linearity of expectation, Markov’s inequality, Chernoff bound
   
   (b) **Alterations**
   Lower bound for the diagonal Ramsey numbers, graph with high girth and high chromatic number
   
   (c) **The Second Moment**
   Chebyshev’s inequality, threshold functions
(d) **The Local Lemma**  
Statement of general case, symmetric case, property B of a hypergraph, lower bounds for diagonal Ramsey numbers

(e) **Correlation Inequalities**  
Ahlswede-Daykin, FKG inequality, Harris’ inequality

(f) **Martingales**  
Azuma’s inequality, vertex and edge exposures

4. Additive Combinatorics

(a) **Sumset Inequalities**  
Real case, exact inverse sumset theorem, Cauchy-Davenport theorem, Rusza triangle inequality, covering lemmas

(b) **Additive Energy**  
Bounds for additive energy, Balog-Szemeredi-Gowers theorem

(c) **Density of Sumsets of Integers**  
Schnirelmann density, Mann’s theorem

(d) **The Sum Product Theorem**  
The sum product theorem, real case, Erdos-Szemeredi sum-product conjecture

(e) **Fourier Methods**  
Parseval’s identity, additive energy in fourier coefficients, Gauss sums, BLR linearity test, formula for the number of 3-arithmetic progressions

(f) **Applications of Szemeredi regularity lemma**  
Triangle removal lemma, Roth’s theorem

(g) **Polynomial methods**  
Combinatorial Nullstellensatz, proof of Cauchy-Davenport theorem, Erdos Heilbronn conjecture

(h) **Waring problem**

(i) **Hindman’s theorem**