

# HOMWORK 5

MATH 435 Geometry  
Fall 2007

10/16/2007. Due on 10/23/2007

**Instructions:** Solve the following problems. Provide as much written detail as possible.

1. Determine the projective Point of intersection of the following two Lines in  $\mathbb{RP}^2$ :

$$\begin{aligned}x + 6y + 3z &= 0 \\2x - 4y - 5z &= 0.\end{aligned}$$

2. Let  $[a : b : c] \in \mathbb{RP}^2$  be a projective point whose representative vector  $(a, b, c)$  has *rational* coordinates  $a, b, c$ . Show that you can find *integers*  $a', b', c'$  so that  $[a : b : c] = [a' : b' : c']$ .
3. Determine an equation for the projective Lines that pass through each pair of different points :  $[1 : 1 : 1], [1 : 0 : 0], [0 : 1 : 0], [0 : 0 : 1]$ .