## Homework 10

1. Find the general solutions to the following ODEs
(a) $y^{\prime \prime}-2 y^{\prime}+2 y=0$
(b) $y^{\prime \prime}+2 y^{\prime}+2 y=0$
(c) $y^{\prime \prime}+25 y=0$
(d) $4 y^{\prime \prime}+16 y^{\prime}+25 y=0$
(e) $4 y^{\prime \prime}-20 y^{\prime}+25 y=0$
(f) $y^{\prime \prime}-6 y^{\prime}+9 y=0$
2. Find the solutions to the following IVPs and state if the solution is growing, steady or decaying
(a) $y^{\prime \prime}+4 y=0, y(0)=0, y^{\prime}(0)=1$
(b) $y^{\prime \prime}-4 y^{\prime}+5 y=0, y(0)=3, y^{\prime}(0)=0$
(c) $y^{\prime \prime}+4 y^{\prime}+5 y=0, y(0)=3, y^{\prime}(0)=0$
3. Find the solutions to the following parameterized IVPs and determine the critical value of $\alpha$ when the long term behavior changes
(a) $y^{\prime \prime}-3 y^{\prime}-4 y=0, y(0)=\alpha, y^{\prime}(0)=2$
(b) $y^{\prime \prime}-4 y^{\prime}+4 y=0, y(0)=1, y^{\prime}(0)=\alpha$
