

Consider a system of  $N$  bosons on the three dimensional unit torus interacting via a pair potential  $N^2V(N(x_i - x_j))$ , where  $x = (x_1, \dots, x_N)$  denotes the positions of the particles. Suppose that the initial data  $\psi_{N,0}$  satisfies the condition  $(\psi_{N,0}, H_N^2 \psi_{N,0}) \leq CN^2$ , where  $H_N$  is the Hamiltonian of the Bose system. Let  $\psi_{N,t}$  denote the solution to the Schrödinger equation with Hamiltonian  $H_N$ . Gross and Pitaevskii proposed to model the dynamics of such system by a nonlinear Schrödinger equation, the Gross-Pitaevskii (GP) equation. The GP hierarchy is an infinite BBGKY hierarchy of equations so that if  $u_t$  solves the GP equation, then the family of  $k$ -particle density matrices  $\{\otimes_k u_t, k \geq 1\}$  solves the GP hierarchy. We prove that as  $N \rightarrow \infty$  the limit points of the  $k$ -particle density matrices of  $\psi_{N,t}$  are solutions of the GP hierarchy. The uniqueness of the solutions to this hierarchy remains an open question. Our analysis requires that the  $N$  boson dynamics is described by a modified Hamiltonian which cuts off the pair interactions whenever at least three particles come into a region with diameter much smaller than the typical inter-particle distance. Our proof can be extended to a modified Hamiltonian which only forbids at least  $n$

particles from coming close together, for any fixed  $n$ .