

1. Use a test or a *combination* of tests from 11.2-11.6 to decide if the series is absolutely convergent (AC), conditionally convergent (CC), or divergent (D).

Your options are: geometric series test, p -series test, divergence test, integral test, direct comparison test, limit comparison test, ratio test, root test, alternating series test.

(a)
$$\sum_{k=1}^{\infty} \frac{\ln k}{k}$$

(b)
$$\sum_{k=1}^{\infty} \frac{k^2}{(k^2 + 3)^{5/2}}$$

(c)
$$\sum_{k=2}^{\infty} \frac{1}{k \ln^2 k}$$

(d)
$$\sum_{k=1}^{\infty} (-1)^k 2^{1/k}$$

(e)
$$\sum_{k=2}^{\infty} \frac{k}{(k-1)!}$$

(f)
$$\sum_{k=1}^{\infty} \frac{(-1)^k \sin(k)}{k^6 + 1}$$

2. Now we will consider an infinite series of *functions* instead of numbers:

$$\sum_{k=1}^{\infty} \frac{(-1)^k x^k}{k 2^k}$$

Think of it as an infinite-degree polynomial. The problem is that the series might converge for some x values and diverge for other x values!

- (a) Plug in $x = 1$ to get a series just of numbers. Use the ratio test to show this series converges.
- (b) Show that your reasoning applies whenever $|x| < 2$.
- (c) Plug in $x = 4$ to get a series just of numbers. Use the ratio test to show this series diverges.
- (d) Show that your reasoning applies whenever $|x| > 2$.
- (e) Plug in $x = 2$. The ratio test fails, so use another test to decide convergence.
- (f) Do the same for $x = -2$? What test did you use?
- (g) Summarize your work: write the set of x values for which the series is convergent.