## Review Problems for exam 1

Note: these problems are in addition to the homework problems.

You can watch the solutions on the posted streaming power points.

1. Let

$$F(x) = \begin{cases} x^3 + A & x \le 2\\ 6x + 1 & 2 < x < 3\\ x^2 + 2 & x \ge 3 \end{cases}$$

- (a) Find the value of A that makes F(x) continuous at x=2.
- (b) For the constant A from (a): is F(x) differentiable at x=2?
- (c) Is F(x) differentiable at x = 3?
- 2. Show that the equation  $x^3 = x^2 + 1$  has at least one solution.
- 3. Use the definition of the derivative as a limit to find the derivative of  $f(x) = \frac{1}{r+2}$
- 4. Find the center and the radius of the circle  $x^2 + y^2 2x + 4y = 0$
- 5. Evaluate each of the following limits.

(a) 
$$\lim_{x \to 3} \frac{\sqrt{x} - \sqrt{3}}{x - 3} + 3x^2$$
 (b)  $\lim_{x \to 0} \frac{\tan(5x)}{\sin(3x)}$  (c)  $\lim_{x \to 3} \frac{|x - 3|}{x^2 - 9}$ 

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(c) 
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6. Find the derivatives of the following functions.

(a) 
$$F(x) = \sqrt{\frac{e^x}{x^2 + 3}}$$
 (b)  $g(x) = 3\cos^4 x \cdot \sin x^9$  (c)  $f(x) = e^{\sin x}$ 

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$$f(x) = e^{\sin x}$$

(d) 
$$h(x) = \left(\frac{x^2 - \ln x}{3x + 2}\right)^9$$
 (e)  $F(x) = \frac{\tan x(x^2 - 4x)}{\ln x}$ 

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7. Let g(x) be a differentiable function such that g(1) = 2, g(2) = 5, g(3) = 7, g(4) = 2, g'(1) = 3, g'(2) = 2, g'(3) = 8, g'(4) = 10. Let  $f(x) = x^2 + x$ .

Find the exact value of: (a) (gf)'(2) (b)  $\left(\frac{f}{g}\right)'(3)$  (c)  $(g \circ f)(1)$ .

(b) 
$$\left(\frac{f}{a}\right)'$$
 (3)

(c) 
$$(g \circ f)(1)$$
.

- 8. Solve  $\log(5x) + \log(x-1) 2 = 0$
- 9. (a) Describe the rectilinear motion given at time t (in seconds) by  $s(t) = 20 + 8t t^2$  (in meters), for  $0 \le t \le 10$ .

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- (b) Find the total distance traveled.
- 10. Find the domain of the function  $f(x) = \ln(x^2 4)$