

## Corrections to “Intro. to Homological Algebra” by C. Weibel

Cambridge University Press, paperback version, 1995

- p.2 line -12:  $d_{n-1}$  should be  $d_n$
- p.4 lines 5,6:  $V - E - 1$  should be  $E - V + 1$  (twice)
- p.4 lines 7,8: all 5 occurrences of  $v_0$  should be replaced by  $v_1$ .
- p.6, line 7 of Def. 1.2.1: “non-abelian” should be “non-additive”
- p.8 diagram: the upper right entry should be  $C_{p+1,q+1}$ , not  $C_{p+1,p+1}$ .
- p.12 line 1:  $B \rightarrow C$  should be  $B \xrightarrow{p} C$
- p.12 line 9: “so is  $\text{coker}(f) \rightarrow \text{coker}(g)$ ” should be “so is  $\text{coker}(g) \rightarrow \text{coker}(h)$ ”
- p.13 line -1:  $Z_{n-1}(b)$  should be  $Z_{n-1}(B)$
- p.15 line 11:  $B(-1)$  should be  $B[-1]$
- p.18 line 3: Replace the sentence “Give an example...” with: “Conversely, if  $C$  and  $H_*(C)$  are chain homotopy equivalent, show that  $C$  is split.”
- p.18 line 18: Replace  $i = 1, 2$  with  $i = 0, 1$
- p.19 line -7: ‘split complexes’ should be ‘exact complexes’
- p.21 Ex.1.5.3: Add extra paragraph: If  $f : B \rightarrow C$ ,  $g : C \rightarrow D$  and  $e : B \rightarrow C$  are chain maps, show that  $e$  and  $gf$  are chain homotopic if and only if there is a chain map  $\gamma = (e, s, g)$  from  $\text{cyl}(f)$  to  $D$ . Note that  $e$  and  $g$  factor through  $\gamma$ .
- p.24 line -7:  $\partial$  should be  $\alpha$
- p.26 line -10: { let }  $C^\infty(U)$  be ... that  $C^\infty$  is a sheaf...
- p.27 line 7: the contour integral should be  $\frac{1}{2\pi i} \oint f'(z)dz/f(z)$ , not  $\frac{1}{2\pi i} \oint f(z)dz$ .
- p.29 line 17: should read “[Freyd, p. 106], every small full abelian subcategory of  $\mathcal{L}$  is equivalent to a full abelian subcategory of the category  $R\text{-mod}$  of modules over the ring”
- p.32 line 1: 2.6.3 should be 2.6.4
- p.33 line -2: after “no projective objects” add “except 0.”
- p.34 line -14 (Ex. 2.2.1): Add this sentence before the hint: “Their brutal truncations  $\sigma_{\geq 0}P$  form the projective objects in  $\mathbf{Ch}_{\geq 0}$ .”
- p.35 line 8: replace “chain map” by “quasi-isomorphism”
- p.37 line 1: delete ‘commutative’
- p.38 Ex.2.2.4: the  $d'$  after ‘i.e.’ should be just  $d$
- p.40 line -8: the map  $F$  should be  $f$
- p.43 Ex. 2.3.8:  $\mathcal{A}^{(I^{op})}$  should be  $(\mathcal{A}^{op})^{(I^{op})}$
- p.44 line 11: ‘gf’ should be ‘ $gf$ ’ (math font)
- p.44 line -9:  $L_i(A)$  should be  $L_i F(A)$
- p.45 line 11: ‘UF’ should ‘ $UF$ ’
- p.47 line 7: In the upper right entry of the matrix, the last term should be  $F'\lambda$ , not  $F'\lambda'$
- p.47 line -6: the  $m^{th}$  *syzygy*
- p.49 line 1:  $L_n(f)$  should be  $L_n F(f)$
- p.49 line -11 (Ex. 2.4.4): Replace “the mapping cone  $\text{cone}(A)$  of exercise 1.5.1” by the following text: “ $\sigma_{\geq 0}\text{cone}(A)[1]$ , where  $\text{cone}(A)$  is the mapping cone of exercise 1.5.1. If  $\mathcal{A}$  has enough projectives, you may also use the projective objects in  $\mathbf{Ch}_{\geq 0}(\mathcal{A})$ , which are described in Ex. 2.2.1.”
- p.50 line -10:  $\text{Hom}_R(, B)$ -acyclic should be  $\text{Hom}_R(A, )$ -acyclic.
- p.55 line -9 to -6: Replace paragraph with:  
We say that  $\mathcal{A}$  satisfies axiom (AB4) if it is cocomplete and direct sums of monics are monic, i.e., homology commutes with direct sums. This is true for  $\mathbf{Ab}$  and  $\mathbf{mod}\text{-}R$ . (Homology does not commute with arbitrary

colimits; the derived functors of colim intervene via a spectral sequence.) Here are two consequences of axiom (AB4).

p.55 line -5: delete “cocomplete” and insert “satisfying (AB4)” before “has enough projectives”

p.56 line 13: (1) and (2) should be switched

p.57 lines 2,-10:  $a$  is the image (‘ $a$ ’ should be ‘ $a$ ’ twice)

p.57 line 4:  $a_{jk} \in A_j$  should be  $a_j \in A_j$

p.58 lines 6–7: Replace the text “If...and” with: Suppose that  $\mathcal{A} = R\text{-mod}$  and  $\mathcal{B} = \mathbf{Ab}$  (or  $\mathcal{A}$  is any abelian category with enough projectives, and  $\mathcal{A}$  and  $\mathcal{B}$  satisfy axiom (AB5)). If”

p.58 line 9:  $F(A)$  should be  $F(A_i)$

p.60–61: several 2-symbol subscripts are missing the comma (e.g.,  $C_{pq}$  means  $C_{p,q}$ ).

p.61 line -7:  $b_{\dots 1}$  should be  $b_{\dots 1}$

p.62 lines 8: Replace the sentence “Finally...acyclic.” with: “Show that  $\text{Tot}^\oplus(D)$  is not acyclic either.”

p.63 lines 15-16: “double complexes” should be “Hom cochain complexes”, and the display should read

$$\text{Tot}\prod\text{Hom}_{\mathbf{Ab}}(\text{Tot}^\oplus(P \otimes_R Q), I) \cong \text{Tot}\prod\text{Hom}_R(P, \text{Tot}\prod\text{Hom}_{\mathbf{Ab}}(Q, I)).$$

p.66 line 9:  $pB = 0$  should be  $pb = 0$ .

p.67 line 5:  $Tor_*$  should be  $Tor_1$

p.70 end of line -11:  $j =$  should be  $i =$

p.73 line 7:  $Tor_m$  should be  $Tor_n$

p.74 Exercise 3.3.1:  $\dots \cong \mathbb{Z}_{p^\infty}$  should be  $\dots \cong (\mathbb{Q}/\mathbb{Z}[1/p]) \times \hat{\mathbb{Q}}_p/\mathbb{Q}$ .

p.74 Exercise 3.3.5: In the display, replace  $A/pA$  with  $A^*/pA^*$  and delete the final ‘= 0’. On the next line (line -1), ‘ $A$  is divisible’ should be ‘ $A^*$  is divisible, i.e.,  $A$  is torsionfree’.

p.77 Proof of 3.4.1: ... applying  $\text{Ext}^*(-, B)$  yields the exact sequence

$$\text{Hom}(X, B) \rightarrow \text{Hom}(B, B) \xrightarrow{\partial} \text{Ext}^1(A, B)$$

so the identity map  $\text{id}_B$  lifts to a map  $\sigma : X \rightarrow B$  when  $\text{Ext}^1(A, B) = 0$ . As  $\sigma$  is a section of  $B \rightarrow X$ , ...

p.77 lines 7–8: ... the class  $\Theta(\xi) = \partial(\text{id}_B)$  ...  $\text{id}_B$  lifts to  $\text{Hom}(X, B)$  iff ...

p.77 line 11:  $\Theta : \xi \mapsto \partial(\text{id}_B)$

p.79 line -6: “ $X_n$  and  $X_n''$  under  $B$ , and let  $Y_n$  be the...copy of  $B$ .” should be “ $X_n$  and  $X_n'$  under  $B$ .”

p.79 line -4 (display):  $Y_n$  should be  $X_n''$

p.82 line 6: ... axiom (AB5\*) (filtered limits are exact), the above proof can be modified to show ...

p.82 line 9: add sentence: Neeman has given examples of abelian categories with (AB4\*) in which Lemma 3.5.3 and Corollary 3.5.4 both fail; see *Invent. Math.* 148 (2002), 397–420.

p.82 line -8: ‘complete’ should be ‘complete and Hausdorff’

p.84 line -8: 1960 is correct; the paper was published in 1962.

p.85 line -4: Then  $\text{Tot}(C) = \text{Tot}^\Pi(C)$  is ...

p.86 line 2: “nonzero columns.” (not rows)

p.86 line 7:  $d^v(a)$  should be  $-d^v(a)$ .

p.89 line 7: replace ‘cohomology:’ with ‘homology (there is a similar formula for cohomology):’

p.89 line 8:  $\} \otimes \{$  should be  $\} \oplus \{$ .

p.90 line 8:  $\prod_{p+q} n-1$  should be  $\prod_{p+q=n-1}$

p.93 line -3: ‘all  $R$ -modules  $B$ ’ should be ‘all  $R$ -modules  $A$ ’

p.95 line 17: ‘the’ (before  $pd_R(P)$ ) should be ‘then’

p.96 line -11: replace ‘integer  $m$ ’ with ‘ $m \neq 0$ ’

p.97 line 14: Add sentence:

“If in addition  $R$  is finite-dimensional over a field then  $R$  is quasi-Frobenius  $\Leftrightarrow R$  is Frobenius.”

p.101 line -5:  $n < \infty$  should be  $d < \infty$

p.102 lines 3,4:  $\leq 1 + n$  should be  $\leq 1 + d$  twice

p.107 line -8: after  $G(R) \leq id(R)$  insert ‘, and  $id(R) = \dim(R)$  by 4.2.7’

p.113 line 13: the final  $H_q(C)$  should be  $H_{q-1}(C)$

p.122 line 9:  $-(r+1)/r$  should be  $-(r-1)/r$

p.124 line 7:  $E_{0n}^\infty$  is a quotient of  $E_{0n}^a$  and each  $E_{n0}^\infty$  is a subobject of  $E_{n0}^a$ .

p.124 line -7:  $0 \rightarrow E_{0n}^2 \rightarrow H_n \rightarrow E_{1,n-1}^2 \rightarrow 0$ .

p.127 line 14 (\*\*):  $(-1)^{p_1}$  should be  $(-1)^{p_1+q_1}$

p.127 line 16: replace “and (\*\*) for every  $r \geq a$ . We shall” by “for every  $r \geq a$ . If the induced product on  $E^r$  satisfies (\*\*) for all  $r \geq a$ , we shall”

p.131 lines 3–4:  $SO(1)$  should be  $SO(2)$  twice

p.131 line 7: Replace “ $H_2(SO(3)) \cong \mathbb{Z}$ , ...isomorphism.” with “ $d^2$  is an injection, and  $H_2(SO(3)) = 0$ .”

p.132 line -3:  $F_s H_n(C)$  should be  $F_s C_n$

p.134 line 8: The filtration on the complex  $C'$  is bounded below, the one on  $C''$  ...

p.135 line 5: although correct as stated, it would be more clear if it read  $E_{pq}^r(F) \cong E_{2p+q,-p}^{r+1}(\tilde{F})$  and  $E_{pq}^r(F) \cong E_{-q,p+2q}^{r-1}(\text{Dec}F)$  so that the substitution  $n = p + q$  is not needed.

p.135 line 12: the superscripts  $r$  should be  $r + 1$ , viz.,

$$\dots E_{p+r}^{r+1}(\text{cone } f) \rightarrow E_p^{r+1}(B) \rightarrow E_p^{r+1}(C) \rightarrow E_p^{r+1}(\text{cone } f) \rightarrow E_{p-r}^{r+1}(B) \dots$$

p.135 line 18: Insert after  $d(c) = 0$ : “(This assumes that (AB5) holds in  $\mathcal{A}$ .)”

p.135 line -13: after ‘exhaustive’ add: “and that  $\mathcal{A}$  satisfies (AB5).”

p.135 line -4: replace text starting with  $E_{p0}^1$  to read:  $E_{p0}^1$  is  $\bar{C}_p = C_p / (F_{p-1}C_p + d(F_p C_{p+1}))$ ;  $\bar{C}$  is the top quotient chain complex of  $C$ , and  $d_{p0}^1 : E_{p0}^1 \rightarrow E_{p-1,0}^1$  is induced from  $d : C_p \rightarrow C_{p-1}$ .

p.136 lines 2–3: the sequence should read  $0 \rightarrow F_{p-1}C \rightarrow C \rightarrow \bar{C} \rightarrow 0$

p.136 line -9,-8: let  $F_{-p}C$  be  $2^p C$  ( $p \geq 0$ ).

p.136 line -7: “Each row” should be “Each column”

p.137 Cor. 5.5.6 should read: If the spectral sequence weakly converges, then the filtrations on  $H_*(C)$  and  $H_*(\hat{C})$  have the same completions.

p.142 line 16: insert ‘if it is regular’ before ‘, and we have’

p.143 line 15:  $H_q(A)$  should be  $H_q(Q)$

p.145 line -10: insert ‘with  $\epsilon d^v = 0$  before ‘such that’

p.152 line 8:  $\xrightarrow{\otimes_S R}$  should read  $\xrightarrow{\otimes_R S}$ .

p.154 line -2:  $\mathcal{E} = \mathcal{E}^{a+1}$  and  $\mathcal{E}^r$  denotes the  $(r - a - 1)^{st}$  derived couple

p.154 line -1:  $j^{(r)}$  has bidegree  $(1 - r, r - 1)$

p.155 line 2: remove  $\xrightarrow{i} D$  from diagram to read:  $E_{pq}^r \xrightarrow{k} D_{p-1,q}^r \xrightarrow{j^{(r)}} E_{p-r,q+r-1}^r$ .

p.155 line 6: starting with  $E^{a+1}$ .

p.158 line -7:  $\ell H_n + T_n$  should be  $\ell H_n + T_n$

p.160 display on line -7: delete ‘ and  $a$  in  $A$ ’

p.163 line -12: (3.2.29) should be (3.2.9)

p.168 line -7:  $NA = 0$  should be  $Na = 0$

p.168 line -1:  $H_{1-n}(G; A)$  should be  $H_{-1-n}(G; A)$

p.173 line -5:  $(\sigma - 1)K$  should be  $(\sigma - 1)L$

p.177 line 7: “given by  $D_a = a^{-1}ga$ ” should read “corresponding to  $= a^{-1}--a$ ”

- p.177 line 13: If  $m$  is odd, every automorphism of  $D_m$  stabilizing  $C_m$  is inner.
- p.179 line -13: all normalized  $n$ -cocycles and  $n$ -coboundaries
- p.179 line -2:  $\psi(1, g) = \psi(g, 1) = 0$  and
- p.180 line +2:  $\psi(1, g) = \psi(g, 1) = 0$  and
- p.185 fourth line of proof of Classification Theorem:  $\beta(1)$  should be  $\beta(1) = 1$
- p.186 line -3:  $b_h g$  should be  $b_h h$ .
- p.184 lines 11–12:  $(1, g)$  should be  $(0, g)$ , and  $(1, h)$  should be  $(0, h)$
- p.191 Cor. 6.7.9: ... of  $G$  on  $H$  induces an action of  $G/H$  on  $H_*(H; \mathbb{Z})$  and  $H^*(H; \mathbb{Z})$ .
- p.191 line -3: complex of (space missing)
- p.193 line 19: delete ' $\beta\sigma = 0$ ' so it reads ' $(\sigma^2 = 0)$ '
- p.193 lines -3, -8; and p.194 line 7: 'cocommutative' should be 'coassociative'
- p.194 line 18 (6.7.16): delete 'normal' before 'subgroup'
- p.194 line 21: Since  $\{H_*(H; A)\}$  is a universal  $\delta$ -functor of  $A$ ,  $tr \dots$
- p.196 line -4: If  $H$  is in the center of  $G$  and  $A$  is a trivial  $G$ -module then  $G/H$  acts trivially ...
- p.197 Example 6.8.5: The two occurrences of  $D_{2m}$  should read  $D_m$  (on the first and last lines).
- p.201 line 11:  $f = f'$  should be  $f_1 = f_2$
- p.201 Exercise 6.9.2: If ... and ... are central extensions, and  $X$  is perfect, show ...
- p.203 lines 1–2: When  $\mathbb{F}_q$  is a finite field, and  $(n, q) \neq (2, 2), (2, 3), (2, 4), (2, 9), (3, 2), (3, 4), (4, 2)$ , we know that  $H_2(SL_n(\mathbb{F}_q); \mathbb{Z}) = 0$  [Suz, 2.9]. With these exceptions, it follows that
- p.206 line 8:  $H_q(S_n(X) \otimes_{\mathbb{Z}} A)$  should be  $H_q(G; S_n(X) \otimes_{\mathbb{Z}} A)$
- p.213 Exercise 6.11.11: ... Show that for  $i \neq 0$ :

$$H^i(G; \mathbb{Z}) = \begin{cases} \mathbb{Z}_{p^\infty} & i = 2 \\ 0 & \text{else.} \end{cases}$$

- p.213 line -13: ' $H^1(G; \mathbb{Z})$  is the group of continuous maps from  $G$  to  $\mathbb{Z}$ ' should be ' $H^1(G; A)$  is the group of continuous homomorphisms from  $G$  to  $A$ '
- p.226: Line 3 of Exercise 7.3.5 should read:  $\delta$ -functors (assuming that that  $k$  is a field, or that  $N$  is a projective  $k$ -module):
- p.234 line 9:  $m^h$  should be  $M^h$
- p.238 lines 4–7: Replace these two sentences (Show that...it suffices to show that  $\dots = 0$ .) by:  
Conversely, suppose that  $\mathfrak{g} = \mathfrak{f}/\mathfrak{r}$  for some free Lie algebra  $\mathfrak{f}$  with  $\mathfrak{r} \subseteq [\mathfrak{f}, \mathfrak{f}]$ , and  $\mathfrak{g}$  is free as a  $k$ -module. Show that if  $H^2(\mathfrak{g}, M) = 0$  for all  $\mathfrak{g}$ -modules  $M$  then  $\mathfrak{g}$  is a free Lie algebra. *Hint*: It suffices to show that  $\dots = 0$ .
- p.255 line -8:  $0 \leq i_s \leq \dots \leq i_1 \leq m$  should be  $0 \leq i_s < \dots < i_1 \leq m$
- p.256 line 8: identity (not identify)
- p.257 line 15 (display):  $\alpha_*(t)$  should be  $\alpha_*(s)$
- p.258 lines 1, 20 and -7: 'combinational' should be 'combinatorial'
- p.261 lines -9, -8, -6: 'combinatorial' is misspelled three more times
- p.262 line 14: [We] first use induction on  $r < k$  ...
- p.262 line 16: replace "If  $r = k$  we set  $g_r = g$ . If  $r \neq k$ " by "For  $r < k$ "
- p.262 line 18:  $g_r = g(\sigma_r u)^{-1}$
- p.262 line 18: replace "The element  $y = g_n$ " by "If  $k = n + 1$ ,  $y = g_n$ . Then insert the text:

For  $k \leq t \leq n + 1$ , we use downward induction on  $t$ , to construct  $g_t \in G_{n+1}$  so that  $\partial_i g_t = x_i$  if  $i < k$  or  $i > t$ ; the element  $y = g_k$  satisfies the Kan condition that  $\partial_i y = x_i$  for  $i \neq k$ . Starting with  $g_{n+1} = g_{k-1}$ , we suppose  $g_{t+1}$  constructed and inductively set

$$z = \sigma_t [\partial_{t+1}(g_{t+1})^{-1} \cdot x_{t+1}].$$

Then  $\partial_i z = 1$  if  $i < k$  or  $i > t + 1$  and  $\partial_{t+1} z = \partial_{t+1} g_{t+1}^{-1} \cdot x_{t+1}$ . Setting  $g_t = g_{t+1} \cdot z$ , it follows that  $\partial_i(g_t) = x_i$  if  $i < k$  or  $i > t$ . This completes the inductive step, and the proof.

p.262 line -13: ‘egery  $n$ ’ should be ‘every sufficiently large  $n$ ’

p.262 line -6:  $\partial_i(y)$  should be  $\partial_i(y) = x_i$

p.264 lines 2–3: the two occurrences of  $S(X)$  should read  $S(|X|)$

p.265 add to end of Exercise 8.3.3:

Extend exercise 8.2.5 to show that a homomorphism of simplicial groups  $G \rightarrow G''$  is a Kan fibration if and only if the induced maps  $N_n G \rightarrow N_n G''$  are onto for all  $n > 0$ . In this case there is also a long exact sequence, ending in  $\pi_0(G'')$ .

p.266 line 14: that  $\sigma_i(x_i) \neq 0$ , then  $y = y - \sigma_i \partial_i y = \sum_{j>i} \sigma_j(x'_j)$ . By induction,  $y = 0$ . Hence  $D_n \cap N_n = 0$ .

p.267 line 5: fix subscript on sum:  $d\sigma_p(x) = \sum_{p+2}^n$

p.267 line 6:  $d\sigma_p^2(x) + \sigma_p d\sigma_p(x) = \sum_{i=p+2}^{n+1} \dots + \sum_{i=p+2}^n$

p.267 line 7:  $= (-1)^p \sigma_p(x)$ .

p.267 line 8: Hence  $\{s_n = (-1)^p \sigma^p\}$

p.268 line -3: ‘ $\{0, 1, \dots, i - 1\}$ ’ should be ‘ $\{0, 1, \dots, i\}$ ’

p.270 line -3: replace “[Dold]” with “[Dold, 1.8]”

p.273: the middle display should read

$$\mathrm{Hom}_{\mathbf{Ch}}(NA, C) \cong \mathrm{Hom}_{S\mathcal{A}}(A, K(C)).$$

p.274 line -12: ‘the zero map’ should read ‘projection onto a constant simplicial subobject.’

p.278 display on line 8: 1 should be subtracted from the subscripts:  $\sigma_{\mu(n)-1}^h \dots \sigma_{\mu(p+1)-1}^h \sigma_{\mu(p)-1}^v \dots \sigma_{\mu(1)-1}^v$

p.280 lines 10–11:  $\eta: 1_C \rightarrow UF$  and ...  $\varepsilon: FU \rightarrow 1_B$ . (switch  $\mathcal{B}$  and  $\mathcal{C}$ )

p.283 line -2:  $\bar{r}_i \bar{r}_{i+1}$  should be  $\overline{r_i r_{i+1}}$

p.287 lines -5, -4: “is an exact sequence” should be “is a sequence” and “is also exact” should be “is exact”

p.290 line before 8.7.9: Insert sentence: The proof of Theorem 3.4.3 goes through to prove that  $\mathrm{Ext}_{R/k}^1(M, N)$  classifies equivalence classes of  $k$ -split extensions of  $M$  by  $N$ .

p.291 line -2: ... to  $(R/I)^d$ . If each  $x_i R \subset R$  is  $k$ -split then:

p.294 line -8: If  $M$  is an  $R$ -module, (‘a  $k$ ’ should be ‘an  $R$ ’)

p.295 line -4 (display):  $D^1(R, M)$  should be  $D^1(R/k, M)$

p.296 8.8.6: “If  $k$  is a field” should be “If  $R$  is a field”

p.297, line -9: the sequence should read

$$\dots \rightarrow D_{n+1}(R/K, M) \rightarrow D_n(K/k, M) \rightarrow D_n(R/k, M) \rightarrow D_n(R/K, M) \rightarrow D_{n-1}(K/k, M) \rightarrow \dots$$

p.298 line 2 of 8.8.7: *Commalg* should be in roman font: **Commalg**

p.301 lines 4–5: the ranges should be “if  $0 < i \leq n$ ” and “if  $i = n + 1$ ” respectively.

p.304 Exercise 9.1.3: the variable  $n$  should  $m$  each time ( $y_n, R^n, n, p < n$ ); and  $x$  (on line 17) should be  $\mathbf{x}$

p.307 line -1 should read:

As  $\mathrm{Tor}_1^{R^e/k}(R^e, M) = 0$ , the long exact relative Tor sequence (Lemma 8.7.8) yields

p.322: On line 1, insert “If  $1/2 \in k$ ,” before “ $\Omega_{R/k}^*$  is the free graded-commutative” and (on line 4) add the sentence: In general,  $\Omega_{R/k}^*$  is the free alternating  $R$ -algebra generated by  $\Omega_{R/k}^1$ .

p.325 line -6:  $(-1)^n$  should be  $(-1)^\sigma$

p.329 line 5: This display should read

$$\mathrm{trace}_n(x \otimes g^1 \otimes \dots \otimes g^n) = \sum_{i_0, \dots, i_n=1}^m x_{i_0 i_1} \otimes g_{i_1 i_2}^1 \otimes \dots \otimes g_{i_r i_{r+1}}^r \otimes \dots \otimes g_{i_n i_0}^n.$$

p.332 lines 12–13: replace with the display

$$\text{trace } e_{\sigma_1, \sigma_2}(r_1) \otimes \cdots \otimes e_{\sigma_n, \sigma_1}(r_n) = r_1 \otimes \cdots \otimes r_n.$$

p.354 line -6: Add sentence: It also follows from the Connes-Karoubi theorem on noncommutative de Rham homology in C.R. Acad. Sci. Paris, t. 297 (1983), p. 381–384.

p.353 line 7:  $u = ce_n$ ” should read ”...  $u = ce_{n+1}$ ”

p.353 line -7: the final term in the display should be  $HC_{n-2}^{(i-1)}(R)$

p.359 Exercise 9.9.5: This is wrong; replace it with:

**Exercise 9.9.5** (Grauert-Kerner) Consider the artinian algebra  $R = k[x, y]/(\partial f/\partial x, \partial f/\partial y, x^5)$ , where  $f = x^4 + x^2y^3 + y^5$ . Show that  $I = (x, y)R$  is nilpotent, and  $f$  is a nonzero element of  $H_{dR}^0(R)$  which vanishes in  $H_{dR}^0(R/I)$ .

p.370 line -6: [ho-]“mopy” should be [ho-]“motopy” and  $b''$  should be  $b'''$ ,

p.375 line 4:  $u\delta = ig : B' \rightarrow B$  should be  $T(u)\delta = ig : B' \rightarrow T(B)$

p.376 line 8: after ‘naturality of the mapping cone construction’ add “and the chain homotopy between  $gu$  and  $u'f$ .”

p.376 line -10: diagram ... commutes up to chain homotopy.

p.381 line 6: ‘(left)’ should be ‘(right)’

p.382 lines-6,-7 (10.3.8): the two occurrences of ‘right’ should be ‘left’

p.383 line 7 (Corollary 10.3.10): after ‘object’ add ‘, and that  $S$  is saturated.’ Add to the end of the proof the sentence: “So  $S$  contains maps  $Y \xrightarrow{0} X \xrightarrow{0} Z$ , and hence  $X \xrightarrow{0} X$ .”

p.384 lines 9, 11: ‘left’ fraction should be ‘right’ fraction

p.384 line 13: Replacing ‘right’ by ‘left’

p.385 line 1:  $\mathcal{B}$  is a small category and  $\text{Ext}(A, B)$  is a set for all  $A \in \mathcal{A}, B \in \mathcal{B}$ . Then show that...

p.386 lines 7–9: six occurrences of  $g$  should be  $v$ : ...there should be a  $v : X \rightarrow Z$ ...  $f - g = uv$ . Embed  $v$  in an exact triangle  $(t, v, w)$  ... Since  $vt = 0$ ,  $(f - g)t = uvw = 0$ , ...

p.386 lines 14–18: Replace the two sentences “Given  $us_1^{-1} : \dots$  triangle in  $\mathbf{K}$ ” with: “The exact triangles in  $S^{-1}\mathbf{K}$  are defined to be those triangles which are isomorphic, in the sense of (TR1), to the image under  $\mathbf{K} \rightarrow S^{-1}\mathbf{K}$  of an exact triangle in  $\mathbf{K}$ .”

p.386 line 20: replace “straightforward but lengthy; one uses the fact” with “straightforward; one uses (TR3) and the fact that...”

p.387 line -12 (10.4.5): delete ‘well-powered’ (Gabber points out that this condition is superfluous).

p.388 lines 2–3: the ‘ $-dky$ ’ and ‘ $+dk$ ’ should be ‘ $+dky$ ’ and ‘ $-dk$ ’

p.396 line 10: [Hart, II.5]

p.396 line 12: [Hart, exercise III.6.4] should be [HartRD, II.1.2]

p.400 line 8: the last two  $(A, B)$  should be  $(A, T^n B)$

p.400 line -7:  $\text{Hom}(-, B)$  should be  $\text{Hom}(-, B)$

p.405 line -2: a natural homomorphism in  $\mathbf{D}(R)$ , which is an isomorphism if either each  $C_i$  is fin. gen. projective or else  $A$  is quasi-isomorphic to a bounded below chain complex of fin. gen. projective  $R$ -modules:

p.420 line 13: in exercise 6.11.3 (not 6.11.4)

p.426 line -5: ‘section 7’ should be ‘section 6’

p.427 line -9: ‘Chapter 3, section 7’ should be ‘Chapter 3, section 5’

p.427 line -1:  $I \in I$  should be  $i \in I$

p.428 line 16:  $F_i \rightarrow F_i \rightarrow C$  should be  $F_j \rightarrow F_i \rightarrow C$

p.429 line 15: ‘Chapter 1’ should read ‘Chapter 2’

p.431 line 6: ‘functions’ should be ‘functors.’

p.435 under ‘AB4 axiom’: add page 55

p.439 add entry to Index under ‘double chain complex’:  
Connes’ —  $\mathcal{B}$ . *See* Connes’ double complex.

p.444, under ‘Lie group’: [page] 158 should be 159

p.445, line -6: ‘Øre’ should be ‘Ore’

p.448 column 2: lines 29-30 should only be singly indented (“— of” refers to spectral sequence)

### References

[EM] Eilenberg, S., and Moore, J. “Limits and Spectral Sequences.” *Topology* **1** (1961): 1–23.