

## Formulas for Exam #1

$$\frac{d}{dx} \sin(x) = \cos(x)$$

$$\frac{d}{dx} a^x = a^x \ln(a)$$

$$\frac{d}{dx} \cos(x) = -\sin(x)$$

$$\frac{d}{dx} x^n = nx^{n-1}$$

$$\mathbf{a} \cdot \mathbf{b} = |\mathbf{a}||\mathbf{b}| \cos \theta$$

$$|\mathbf{a} \times \mathbf{b}| = |\mathbf{a}||\mathbf{b}| \sin \theta$$

The vector equation for a line with direction  $\mathbf{v}$  which passes through a point  $\mathbf{r}_0$  is:

$$\mathbf{r}(t) = \mathbf{r}_0 + t\mathbf{v}$$

The equation of a the plane tangent to  $z = f(x, y)$  at the point  $(x_0, y_0, z_0)$  where  $z_0 = f(x_0, y_0)$  is:

$$(z - z_0) = f_x(x_0, y_0)(x - x_0) + f_y(x_0, y_0)(y - y_0)$$

The distance from the point  $P(x_1, y_1, z_1)$  to the plane  $ax + by + cz + d = 0$  is:

$$\frac{|ax_1 + by_1 + cz_1 + d|}{\sqrt{a^2 + b^2 + c^2}}$$

$$\text{comp}_{\mathbf{a}} \mathbf{b} = \frac{\mathbf{a} \cdot \mathbf{b}}{|\mathbf{a}|}$$

$$\text{proj}_{\mathbf{a}} \mathbf{b} = \frac{(\mathbf{a} \cdot \mathbf{b})}{(\mathbf{a} \cdot \mathbf{a})} \mathbf{a}$$

$$\mathbf{a} \times (\mathbf{b} \times \mathbf{c}) = (\mathbf{a} \cdot \mathbf{c})\mathbf{b} - (\mathbf{a} \cdot \mathbf{b})\mathbf{c}$$

$$\mathbf{a} \cdot (\mathbf{b} \times \mathbf{c}) = (\mathbf{a} \times \mathbf{b}) \cdot \mathbf{c}$$

$$s(t) = \int_a^t |\mathbf{r}'(t)| dt$$

Curvature for  $\mathbf{r}(t)$

$$\kappa = \left| \frac{d\mathbf{T}}{ds} \right| = \frac{|\mathbf{T}'(t)|}{|\mathbf{r}'(t)|} = \frac{|\mathbf{r}'(t) \times \mathbf{r}''(t)|}{|\mathbf{r}'(t)|^3}$$

Curvature for a plane curve  $y = f(x)$

$$\kappa = \frac{|f''(x)|}{[1 + (f'(x))^2]^{\frac{3}{2}}}$$

$$\mathbf{T}(t) = \frac{\mathbf{r}'(t)}{|\mathbf{r}'(t)|}$$

$$\mathbf{N}(t) = \frac{\mathbf{T}'(t)}{|\mathbf{T}'(t)|}$$

$$\mathbf{B}(t) = \mathbf{T}(t) \times \mathbf{N}(t)$$

$$a_{\mathbf{N}} = \frac{|\mathbf{r}'(t) \times \mathbf{r}''(t)|}{|\mathbf{r}'(t)|}$$

$$a_{\mathbf{T}} = \frac{\mathbf{r}'(t) \cdot \mathbf{r}''(t)}{|\mathbf{r}'(t)|}$$

Consider the level surface  $F(x, y, z) = K$ ,  $K$  a constant. Then,

$$\frac{\partial z}{\partial x} = -\frac{F_x}{F_z}$$

$$\frac{\partial z}{\partial y} = -\frac{F_y}{F_z}$$

$$\nabla f(x, y, z) = f_x \mathbf{i} + f_y \mathbf{j} + f_z \mathbf{k}$$