

MATH 583, Dr. Z. , **Problem Set #3**, Mon., Mar. 10, 2003.

Due: Mar. 24, 2003.

**Theory:**

- 1) Compute  $s_{(3,2)}(x_1, x_2)$  in three different ways (from the definition as a certain determinant divided by the discriminant, from (3.4), and from 3.5.)
- 2) Test ex. 1 of section 3 with  $\lambda = (3, 2)$ , using problem 1.
- 3) For  $n = 4$ , compute the  $p(4)$  by  $p(4)$  matrix  $\langle h_\lambda, h_\mu \rangle$ , for  $\lambda, \mu$  partitions of 4. (Hint, first express one of the  $h$ 's in terms of  $m$ 's.)
- 4) Repeat 3) by expressing both  $h$ 's in terms of  $p$ 's.

**Maple**

- 1) Write a Maple procedure to verify ex. 6 of section 4 (p. 38) for general  $n$ . Run the program for  $n \leq 6$ .
- 2) Write a Maple procedure  $\text{IP}(f, g, \mathbf{x}, \mathbf{n})$ , that inputs two symmetric polynomials in  $(x[1], \dots, x[n])$  (first the program has to check that  $f$  and  $g$  are indeed symmetric), and outputs the inner-product  $\langle f, g \rangle$ . You may load, and use, the current version of SF.